1/8

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Studying the kinetics and mechanism of tartrazine removal by activated carbon under the influence of shaking speed using Diffusion-Binding model

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Abstract

The kinetic and mechanistic study of the removal rate of tartarzine by adsorption onto activated carbon under the influence of shaking speed is presented in this work. Diffusion binding model (DB-model) and pseudo second order model (PSO-model) were applied for suggesting the dependency of surface-reaction (solute or active site) and to give the main outputs; adsorption rate constants and capacities. According to error evaluation of both models, it was found that DB-model is more representative for tartarzine activated carbon adsorption system than PSO-model and it is suggested that surface-reaction kinetic is dependent on tartrazine concentration not on active sites of adsorbent. In addition, DB-model showed that adsorption rate constants and capacities increase with shaking speed which agrees with the fact of enhancing some diffusion steps because of shaking. DB-model, as a diffusion model as well, was applied to investigate diffusion mechanistic and it was concluded that for static condition (shaking speed = 0 rpm), adsorption passes two stages, the first is controlled by bulk-diffusion and film-diffusion and the second is controlled by intraparticle-diffusion. For shaking speeds 25 rpm and 50 rpm, bulk-diffusion and filmdiffusion almost have no contribution in controlling overall rate and consequently intraparticle-diffusion is the controlling step. For shaking speeds from 75 to 125 rpm, intraparticle-diffusion is suggested to have strong contribution in controlling adsorption process.

Keywords:

Kinetics, adsorption, diffusion, DB-model, tartrazine, activated carbon.

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1. Introduction

Adsorption process is employed extensively for contaminant separation in environmental engineering. Adsorption becomes effective by using porous adsorbents because of remarkable high surface area. Contaminant adsorption onto porous adsorbent is always accompanied by diffusion mechanisms which have a significant effect on adsorption rate [1].

Conducting investigation to determine the effectiveness of any adsorption system requires kinetic modeling to determine capacity and rate constant and in addition to understand the mechanism of the adsorption process. There are many kinetic models which are successful in predicting batch adsorption behavior. Kinetic modeling can be performed according to surface-reaction models and diffusion models. Surface-reaction models concern the nature of binding. Diffusion models investigate the mechanistic steps of adsorption process. In the absence of agitation/stirring/shaking, the removal rate of contaminant is dependent on the rate of external mass transfer and intra-particle transport [2]. External mass transfer in many cases is faster than intra-particle transport, thus the rate of adsorption in porous adsorbents is generally controlled by intra-particle diffusion within the pores network. In the presence of effective agitation, external mass transfer enhances and intraparticle-diffusion is considered to control adsorption rate [3,4]. Furthermore, intraparticle-diffusion may occur by several different rates depending on pore size distribution [5,6]. Diffusion behavior may therefore be determined by modeling the experimental uptake points to proper applied kinetic model.

For comprehensive study, an accustomed practice in many adsorption works is to apply the two types of modeling; surface-reaction and diffusion. The present work introduces the recently developed DB-model to determine adsorption rate behavior of tartrazine onto activated carbon (T/AC) under the influence of different shaking speeds (SH-S) according to two aspects; surface-reaction and diffusion. DB-model surface-reaction modeling indicates that DB-model is better representing T/AC adsorption system than PSO-model. Diffusion modeling by DB-model gives important information about diffusion mechanistic of T/AC adsorption system.

2. Kinetic models 2.1. DB-model

DB-model has been recently presented and its main postulations are the dependency of adsorption on the solute concentration and the effectiveness of diffusion during adsorption process. DB-model is applied according to its linear form [7]:

$$\frac{C_{\rm f}C_{\rm e}}{C_{\rm i}}\ln C_{\rm t} - C_{\rm t} = St^n - D, \qquad \text{and slope, } S = k_{\rm DB}/n \qquad (1)$$

where C_i : initial concentration, C_f : final concentration , C_e : equilibration concentration, and C_i : concentration at any time *t* and where *S*, *n*, k_{DB} and *D* are equation-slope, time-power (n < 1), rate constant and integration constant respectively. The constant of equation (1) *D* can be calculated according to the following expression [7]:

$$D = \frac{C_{\rm f}C_{\rm e}}{C_{\rm i}}\ln C_{\rm i} - C_{\rm i}$$
⁽²⁾

Plotting of $\ln[(C_f C_e/C_i)\ln C_t - C_t]$ against t^n should produce a line from which the adsorption rate constant (k_{DB}) and estimated adsorption capacity of DB-model (q_{DB}) can be calculated according to the following two expressions respectively [7]:

 $k_{\rm DB} = S \times n \qquad ({\rm mg.l}^{-1}.{\rm min}^{-n}) \tag{3}$

 $q_{\rm DB} = S \times t^n \times V/m \qquad (\rm mg.g^{-1}) \tag{4}$

where V is the solution volume and m is the used adsorbent mass. In this work; C, V, m and t have the following units respectively; ppm, l, g, and minute.

Applying eqn. (1) on system's kinetic data points should give a linear plot of $((C_f C_e/C_i) \ln C_t - C_t)$ against t^n . The linearity is achieved under the condition of properly selecting the value of the power *n* by using a data sheet program. The proper selection of *n*-value should give the highest determination coefficient, R^2 , of regressed line and in the same time the program-calculated value of the constant *D* should be equal or very close to $((C_f C_e/C_i) \ln C_i - C_i)$ according to eqn. (2).

2.2. PSO-model

PSO-model is widely applied to describe the adsorption kinetics of many different adsorption systems. Its major proposals are dependency of adsorption rate on vacant adsorbent-sites and the chemi-sorption nature of the adsorption processes. PSO-model has the following known linear expression [8]:

$$\frac{t}{q_{t}} = \frac{1}{k_{\rm PSO}q_{\rm PSO}^{2}} + \frac{t}{q_{\rm PSO}}$$
(5)

where q_{PSO} and q_t (mg.g⁻¹) are the amounts of contaminant removed by adsorbent at equilibrium and at time *t*, respectively and k_{PSO} (g.mg⁻¹.min⁻¹) is the adsorption rate constant according to PSO-model.

2.3. Error determination

To evaluate applied kinetic models for selecting the proper one to represent adsorption system under study, determination coefficient (R^2) of linear regression was considered. In addition relative error in estimating adsorption capacity (RE%) was also considered and was calculated according to the followinfg expression [9]:

$$RE\% = 100 \times (q_{\exp} - q_{\text{model}}) / q_{\exp}$$
(6)

3. Experimental

3.1. Tartrazine solution and Activated carbon

Tartrazine (molecular formula: $C_{16}H_9N_4Na_3O_9S_2$) was supplied by Morgan Chemical Company and were used without further purification. Tartrazine (100 mg) was applied into deionized water to prepare 100 ppm working solution and pH was adjusted to be 6.8. Activated carbon was also supplied by Morgan Chemical Company and has been used as adsorbent without further chemical treatment. A measured quantity of activated carbon was immersed in hot water for three hours to remove some potential contamination. The washed

| Proceeding of the 7 th ICEE Conference 27-29 May 2014 | CEEB-1 | 4 / 8 |
|--|--------|-------|
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activated carbon was filtered and oven dried at 60° C for 2 hours and then heated to 200 °C for 3 hours with flow of N₂ to hinder oxidation by air.

3.2. Batch adsorption experiments

SH-S is the factor to study in this work (0, 25, 50, 75, 100, 125 rpm). For each experiment, tartarzine solution (100 ml) was treated by active carbon (0.5 g) with applied temperature (25°C) at selected SH-S using Companion SI 300R shaker. Periodically, every 10 minutes, 3 ml was withdrawn from solution flask for absorbance measurement (at λ_{max} =425) using Agilant UV-Vis Cary 60PC scan spectrophotometer using glass cell of 1 cm width.

4. Results and discussion

4.1 General comments on adsorption behavior

Fig. 1 shows the change of removal percentage (R%) of tartrazine with time. Adsorptiveremoval of is gradual and smooth for all applied SH-S and as SH-S increases removal percentage increases. This is an important phenomenon points to the remarkable effect of shaking on the adsorption effectiveness and it can be related to the enhancement of diffusion rates due to influencing the distribution of solute in bulk solution and decrease the resistance of the boundary film [2,3].

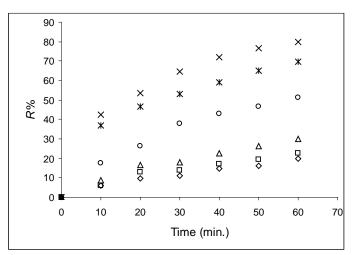


Fig. 1. Change of removal percentage of tartrazine with time for SH-S: 0 (\Diamond), 25 (\Box), 50 (Δ), 75 (o), 100 (*), 125 rpm (×)

4.2. Surface-reaction modeling: Application of DB-model and PSO-model

Fig. 2 shows the kinetic plots of T/AC adsorption system by modeling using DB-model and PSO-model. The outputs of these plots were calculated and are given in Table 1.

5/8

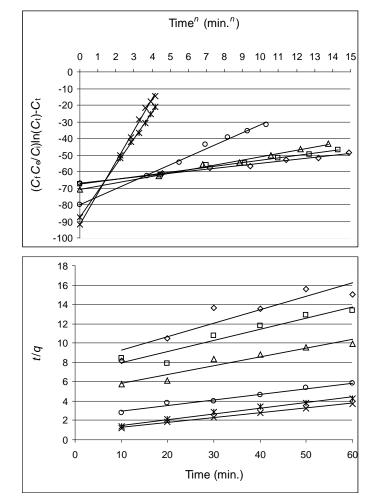


Fig. 2. Plots of DB-model (A)and PSO-model (B) for SH-S: 0 (\Diamond), 25 (\Box), 50 (Δ), 75 (o), 100 (*), 125 rpm (×)

Table 1: Outputs of modeling by DB-model and PSO-model

| | EXP. | DB-model | | | | | PSO-model | | | | |
|------|--------------|----------|-----------------|-------------|-------|--------|--|------------------|-------|--------|--|
| SH-S | q exp | n | k _{DB} | $q_{ m DB}$ | RE% | R^2 | $\begin{array}{c} \boldsymbol{k_{\text{PSO}}} \\ (\times 10^{-3}) \end{array}$ | q _{PSO} | RE% | R^2 | |
| 0 | 4.00 | 0.66 | 0.7763 | 3.51 | 12.25 | 0.9891 | 2.5197 | 7.12 | 78.00 | 0.8561 | |
| 25 | 4.48 | 0.65 | 0.9324 | 4.11 | 8.26 | 0.9873 | 1.9780 | 8.62 | 92.41 | 0.9075 | |
| 50 | 6.02 | 0.64 | 1.2811 | 5.50 | 8.64 | 0.9922 | 1.6904 | 10.98 | 82.39 | 0.9231 | |
| 75 | 10.24 | 0.57 | 2.7322 | 9.89 | 3.42 | 0.9927 | 1.4804 | 16.98 | 65.82 | 0.9829 | |
| 100 | 13.96 | 0.35 | 5.5076 | 13.19 | 5.52 | 0.9993 | 3.6425 | 17.15 | 22.85 | 0.9856 | |
| 125 | 15.98 | 0.35 | 6.5646 | 15.72 | 1.63 | 0.9981 | 3.2797 | 19.92 | 24.66 | 0.9956 | |

From Table 1, referring to determination coefficient values (R^2) of both models, it can be concluded that DB-model is better to represent adsorption kinetics of T/AC adsorption system than PSO-model. In addition, referring to relative error values of adsorption capacity of both models (*RE*%), the estimated adsorption capacities by DB-model are also more accurate than those estimated by PSO-model. Accordingly, it is suggested that surface-interaction of T/AC adsorption system is dependent on tartrazine concentration not on vacant active sites of adsorbent as PSO-model may indicate [7,8]. This suggestion can be supported by recalling that the product of sample volume (*V*) and concentration (*C*) is higher than the product of adsorbent mass (*m*) and sorption capacity (*q*) for all applied SH-H settings. According to DB-model, *n*-values are less than 1 and this indicates remarked contribution of diffusion mechanisms in the adsorption process for all applied SH-S [7]. Furthermore, from table, as SH-S increases from 0 to 125 rpm, *n*-value decreases from 0.66 to 0.35 which indicates increase of contribution of diffusion mechanisms in controlling overall rate of adsorption. This can be understood from the fact that adsorption amount increases with SH-S and this means more accommodation of tartrazine into deep carbon pores which requires more intraparticle diffusion. The rate constant of DB-model increases regularly from 0.7763 to 6.5646 with SH-S. This significant increase suggests that rate constant is not only dependent on surface-reaction but also depends on enhanced diffusion.

4.3. Diffusion modeling: Application of DB-model

DB-model was empirically developed considering the assumption that diffusion has contribution in adsorption process. This was presented by considering proportionality with t^n . Hence; this model is able to recognize diffusion mechanism as presented in the previous section. However, the model can further give some more detailed information about diffusion mechanism when applied considering segmentation of adsorption period into observed stages. Fig. 3 shows DB-model plots according to this application by dividing adsorption whole period into two stages, solid line represents first stage and dashed line represents second stage. The outputs of these plots are summarized in Table 2.

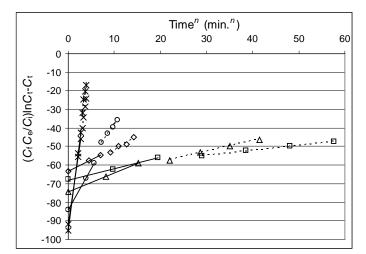


Fig. 3. Plots of DB-model considering segmentation for SH-S: 0 (\diamond), 25 (\Box), 50 (Δ), 75 (o), 100 (*), 125 rpm (×)

For adsorption processes on porous adsorbents, diffusion mechanisms contribute effectively in the overall adsorption rate [10,11]. The steps that contribute in adsorption processes commonly considered as follows: (I) bulk-diffusion, (II) film-diffusion, (III) intraparticlediffusion and finally (IV) surface-reaction [10]. From Table 2, for SH-S= 0 rpm adsorption amount is the lowest and rate constants of both stages are almost similar and n= 0.65. This means that both external diffusion rate (bulk-diffusion and film-diffusion) and intraparticlediffusion rate are of the similar speed and slower than surface reaction step and consequently control the overall rate of adsorption [11]. For SH-S= 25 rpm and 50 rpm, \approx 1 which s indicate that external diffusion is of the same order of surface-reaction. however, rate constant of second stage is about half that of the first stage and consequently intraparticle-diffusion controls the rate during the second stage and this was determined from table 1 as $n\approx$ 0.65 and 0.64 [12]. For SH-S= 75 rpm, $n\approx$ 0.58 and rate constants of the two stages are almost similar

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|---|--|--------|-------|
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and in addition rate constant of the second stage is considerably higher than corresponding rate constants of SH-S < 75 rpm. This indicates that intraparticle-diffusion of the second stage becomes more controlling. For SH-S= 100 rpm and 125 rpm, n \approx 0.33, rate constants of the two stages are almost similar and in addition rate constant of the second stage is considerably higher than corresponding rate constants of SH-S < 100 rpm which indicates that intraparticle-diffusion of the second stage becomes more and more controlling [13].

Another important feature is that the second stage shares significantly in the amount adsorbed. Adsorbed amounts during second stage have a range from 27% to 54% of the total capacities which means that during second stage intraparticle-diffusion is responsible for controlling the overall rate of adsorption.

| GTL G | EXP. | DB-model | | | | | | | | |
|-------|-------------------------|----------|--------------------|--------------------|--------------------|----------------------|--------------|--------------------|----------------------|----------------------|
| SH-S | <i>q</i> _{EXP} | п | k _{DB-S1} | k _{DB-S2} | q _{DB-S1} | $q_{\mathrm{DB-S2}}$ | $q_{\rm DB}$ | RE _{DB} % | $R^2_{\text{DB-S1}}$ | $R^2_{\text{DB-S2}}$ |
| 0 | 4.00 | 0.65 | 0.8078 | 0.9582 | 1.74 | 2.15 | 3.89 | 2.75 | 1.0000 | 0.9632 |
| 25 | 4.48 | 0.99 | 0.5992 | 0.2650 | 2.35 | 2.04 | 4.39 | 2.01 | 0.9981 | 0.9978 |
| 50 | 6.02 | 0.91 | 0.9174 | 0.5238 | 3.08 | 3.02 | 6.10 | 1.33 | 1.0000 | 0.9974 |
| 75 | 10.24 | 0.58 | 2.5974 | 2.0018 | 5.09 | 3.50 | 8.59 | 16.11 | 1.0000 | 0.9977 |
| 100 | 13.96 | 0.33 | 5.6054 | 6.8026 | 9.13 | 4.84 | 13.97 | 0.07 | 1.0000 | 0.9987 |
| 125 | 15.98 | 0.33 | 6.4921 | 6.0707 | 10.57 | 4.32 | 14.89 | 6.82 | 1.0000 | 0.9853 |

Table 2: Outputs of diffusion modeling by DB-model

5. Conclusion

The kinetics and mechanism of T/AC adsorption system has been presented. From surfacereaction kinetic discussion, DB-model was found to be more representative than PSO-model suggesting that adsorption is dependent on tartrazine concentration. Adsorption capacity and rate constant increase regularly and significantly with SH-S indicating enhancement in diffusion because of shaking, however, diffusion becomes more controlling the overall rate due to more contribution of intraparticle-diffusion in adsorption process. Diffusion mechanistic discussion revealed that for low SH-S, both external diffusion rate and intraparticle-diffusion rate control the overall rate of adsorption. For mid SH-S (25-50 rpm), intraparticle-diffusion strongly controls the overall rate of adsorption. In general DB-model successfully represents T/AC adsorption system according for both surface-reaction and diffusion aspects.

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